Calculation policy: Guidance

See PA planning document for WAGBA's and a more detailed breakdown of calculation progression.



Addition

Key language: sum, total, parts and wholes, plus, add, altogether, more, 'is equal to', 'is the same as' and regrouping.

	same as' and regrouping.				
	Progression	Concrete	Pictorial	Abstract	
/Year 1	1.1 Combining two parts to make a whole. https://www.youtube.com/watch?v= 5DgHrfUPVfg		4 + 3 = 7 Four is a part, 3 is a part and the whole is seven.	4 + 3 = 7 Four is a part, 3 is a part and the whole is seven.	
		Counting on using number lines, cubes or Numicon. 4 5 6	Abarmodel which encourages the children to count on, rather than count all.	The abstract number line: 4+2 = 6	
EYFS / \	1.3 Regrouping to make 10 using ten frames or Numicon. https://www.youtube.com/watch?v=m WPgqkO6BTk	6 + 5	Children to draw the ten frame and counters/cubes.	Children to develop an understanding of equality e.g. $6+\Box=11$ $6+5=5+\Box$ $6+5=\Box$	

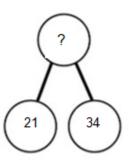
	2.1 Adding three single digits. https://www.youtube.com/watch?v=f Gv 07qomhE	Using Numicon or ten frames. 7+3+4	Using pictures of ten frames or number line. 7 + 3 + 4 0 1 2 3 4 5 6 7 8 9 10 11 12 13 7 15 16 17 18 19 20	Use number bonds to make ten. 6 + 7 + 4 = 6 + 4 + 7 = 17
Year 2	2.2 Use dienes to add two numbers. (2 digit + 1 digit and 2 digit + 2 digit) https://www.youtube.com/watch?v=e0 WrQKR V 8	Continue to develop understanding of partitioning and place value. 41 + 8	Children to represent the dienes e.g. lines for tens and dot/crosses for ones.	41 + 8 Add the ones: 1 + 8 = 9 Add the tens: 40 + 9 = 49
	2.3 Use dienes to add two numbers with regrouping. (2 digit + 1 digit and digit + 2 digit) https://www.youtube.com/watch?v=edfj 5ac1xzQ	36+25 (regrouping in the ones) 10s	36 + 25 10s s 111 11 1 1 1 1 1 1 1	Expanded method: 36 + 25 Add the ones: 6 + 5 = 11 Add the tens: 30 + 20 = 50 50 + 11 = 61
ar 3	3.1 Column method- regrouping (up to 3 digits). Using dienes. https://www.youtube.com/watch?v=7q0 Qm17tP5w	153 + 371 = 524 Hundreds Tens Ones	153 + 371 = 524	Introduce formal method: 153 + 371 524 1
Yea	3.2 Column method- regrouping (up to 3 digits). Using place value counters. https://www.youtube.com/watch?v=Uklrv-3KIgo	243 + 368 = 611 100s 10s 1s 6 1	243 + 368 =611	243 +368 611

Year 4	4.1 Column method- regrouping (up to 4 digits). Using place value counters. https://www.youtube.com/watch?v=_l _nhABeknc	2162 + 1253	2162 + 1253	2162 + 1253 3515
r 5	5.1 Column method- regrouping with more than 4 digits	See Year 4 if required.	See Year 4 if required.	1720cm 750cm + 1500cm 3970cm 1
Year	5.2 Column method — decimals (up to 2 d.p.). Use place value counters. https://www.youtube.com/watch?v=vxK4 rC26Gig	1.36 + 2.37 Ones tenths hundredths and a large and a	1.36 + 2.37 Ones tenths hundredths O O O O O O O O O O O O O O O O O O O	£1.36 + £2.37 £3.73
Year 6	6. 1 Column method- regrouping with more than 4 digits	See Year 4 if required.	See Year 4 if required.	1720cm 750cm + 1500cm 3970cm
\	6.2 Column method – decimals (up to 2 d.p.). Use place value counters.	See Year 5 if required.	See Year 5 if required.	£1.36 + £2.37 £3.73

Conceptual variation; different ways to ask children to solve 21 + 34

Visual representations:

Part-part-whole diagrams and bar models.



	?
21	34

Word problems:

In year 3, there are 21 children and in year 4, there are 34 children. How many children intotal?

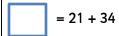
Calculate the sum of twenty-one and thirty-four.

Different forms of equations:

21

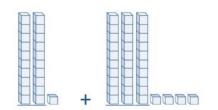
<u>+34</u>

21 + 34 =



21 + 34 = 55. Prove it

Concrete representations:



Missing digit problems:

10s	1s
10 10	0
10 10 10	?
?	5 -

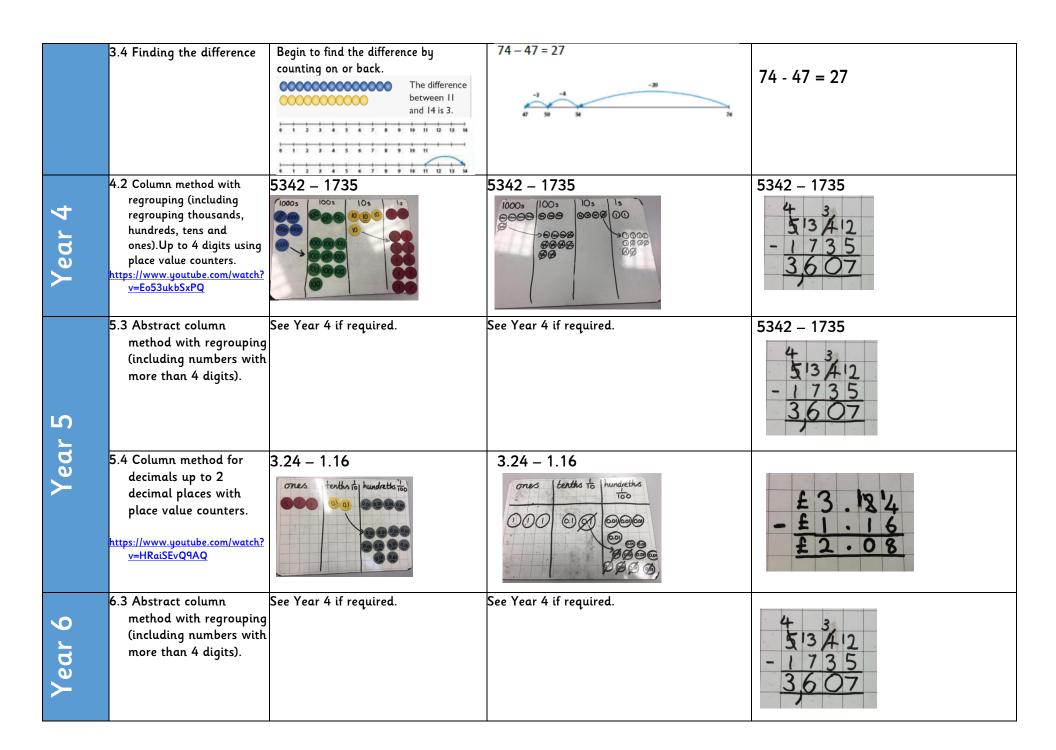
Subtraction language: take away, less than, difference, subtrac



Key language: take away, less than, difference, subtract, minus, fewer, decrease.

	Progression	Concrete	Pictorial	Abstract
1	3	a whole.	Children to draw the concrete resources they are using and cross out the correct amount. The bar model can also be used.	4 - 3 =
EYFS / Year	number line.	Counting back (using number lines or number tracks) children start with 6 and count back 2. $6-2=4$ 1 2 3 4 5 6 7 8 9 10	6-2=4	6 - 2 = 4
	counting on.	Numicon or Cuisenaire rods).	Children to draw the concrete resources they have used or used a bar model to illustrate what they need to calculate.	Find the difference between 8 and 5. $5 + 3 = 8$

	1.7 Make 10 using the ten frame	Making 10 using a ten frame. 14 - 5	Children to present the ten frame pictorially and discuss what they did to make ten.	Children to show how they can make ten by partitioning the smaller number.
	https://www.youtube.com/watch? v=gEgyUQXbbKA			14 - 5 = 9 4 1 14 - 4 = 10 10 - 1 = 9
	2.4 Counting back using a number line. https://www.youtube.com/watch?v=rGZGcw5Vc7Q	15 - 7	15 - 7 = 8 -2 -5 8 10 15	15 – 7 = 8
Year 2		Column method using dienes. 48 - 7 10s 1s 1s 4 1	Children to represent dienes pictorially.	48 – 7 = 41
	2.6 Use dienes to subtract numbers up to 2 digits (with regrouping). https://www.youtube.com/watch?v=Dyj7hvjbImU	Column method using dienes. 41-26 10s 1s 10s 1s 10s 1s 1s 10s 1s	10s 1s 1+1Q	41 – 26 = 15
Year 3	3.3 Column method with regrouping— with place value counters and dienes up to 3 digits. https://www.youtube.com/watch? v=2Rv1TaN-JOw https://www.youtube.com/watch? v=nqVjoR1yXdY	Column method using place value counters. 234 - 88 100s 10s 1s 100s 10s 1s 100s 10s 1s	234-88 100s 10s 1s 000 0000 4 6	Formal column method. 234 - 88 - 6



6.4 Column method for decimals up to 2 decimal places with place value counters

See Year 5 if required.

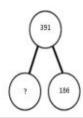
See Year 5 if required.

See Year 5 if required.

Conceptual variation; different ways to ask children to solve 391 - 186

Visual representations:

Part-part-whole diagrams and bar models.



391 186 ? Word problems:

Raj spent £391, Timmy spent £186. How much more did Raj spend?

Calculate the difference between 391 and 186.

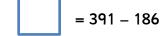
<u>Different forms of equations:</u> 391

<u>-186</u>

What is 186 less than 391?

Missing digit calculations





Concrete representations:



The difference between 11 and 14 is 3.

Multiplication





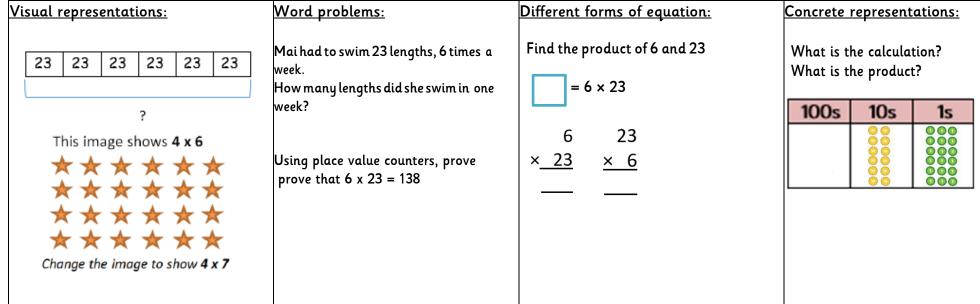
	Progression	Concrete	Pictorial	Abstract
	1.8 Counting in multiples (skip count in 2's, 5's and 10's)	MARIA	0 2 4 6 8	"5, 10, 15, 20, 25"
		The All She and	0 5 10 15 20 25	
		€ € € € € € € € € € € € € € € € € € €	22 22 23 24 25 26 27 28 29 36 31 32 33 45 50 43 73 39 46 41 62 63 44 56 64 74 46 47 56 51 52 53 54 55 65 57 58 59 46 51 62 63 64 65 65 67 68 59 46 51 72 73 74 75 76 77 78 79 46 51 62 63 64 65 66 78 68 99 46 51 62 63 64 65 66 78 68 99 36 51 62 63 64 65 66 78 68 99 36	
1/ EYFS	1.9 Doubling https://www.youtube.com/watch? v=gwDkWu8mgfo			3 + 3 = 6
Year		Repeated addition. 3 × 4 4 + 4 + 4 There are 3 equal groups, with 4 in each group.	picture and use a bar model.	3 × 4 = 12 4 + 4 + 4 = 12

	1.11 Arrays	Putting objects into arrays.	Children describe arrays in different ways.	Children to be able to use an array to write a range
	https://www.youtube.com/watch? v=f3p4_5ast-4		2 groups of 5 5 groups of 2	of calculations e.g. $5 \times 2 = 10$ $2 \times 5 = 10$
.r 2	2.7 Number line to show repeated addition https://www.youtube.com/watch? v=RsBIrg1ujgc	Number lines to show repeated groups. E.g. 3 × 4 Cuisenaire rods and Numicon can be used too.	Represent this pictorially alongside a number line	4 + 4 + 4 = 12 3 × 4 = 12
Year	2.8 Arrays - showing commutative multiplication https://www.youtube.com/wat ch?v=t2q9ePsDwDg	Use arrays to illustrate commutativity counters and pegs can be used. 2 × 5 = 5 × 2 2 lots of 5 5 lots of 2	Children to represent the arrays pictorially. 2 x 5 5 x 2	Children to be able to use an array to write a range of calculations e.g. $10 = 2 \times 5$ $5 \times 2 = 10$ $2 + 2 + 2 + 2 + 2 = 10$ $10 = 5 + 5$
Year 3		Partition to multiply using dienes of Numicon.	A number line should also be used	Children to be encouraged to show the steps they have taken. 4 × 15 10 5 4 × 5 = 20 4 × 10 = 40 60

		,		,
	3.6 Short multiplication (2 digit X 1 digit)	Short multiplication method. Use counters or dienes. 3 X 23	10s Is 00 000	Children to be encouraged to show the steps they have taken. 3 X 3 = 9
	https://www.youtube.com/watch? v=vhH -xViOfQ	6 9	00 000	$3 \times 20 = \frac{60}{69}$ $\times 3$ $\overline{69}$
	3.7 Short multiplication	Formal column method with place value	6 X 23	Formal written method
	with regrouping (2 digit X 1 digit) https://www.youtube.com/watch?v=DPhXev2lb2I	counters. 6 x 23 100s 10s 1s 100s 10s 1s	100s 10s 1s	$6 \times 23 =$ 23 $\frac{\times 6}{138}$
	• • • • • • • • • • • • • • • • • • •	225 X 3 = 675	225 X 3 = 675	1 1
	place value counters. (2 and 3 digit X 1 digit) https://www.youtube.com/watch? v=G3gRW-2ZB k	100's 10's 1's	100s 10s 15 000000 000000000000000000000	225 × 3 = 6 75 h † ° 225 × 3 6 7 5
4	4.4 Grid method to expanded method. (for 2- digit X 2-digit)	Use abstract methods.	Use abstract methods.	First introduce children to the grid method. 56 x 27= 1512
Year	https://www.youtube.com/watch? v=anfh2w0wrz8			× 20 7 50 1000 350 1350 6 120 42 162 1
				Then <u>progress</u> to the expanded method. 56 x 27 42 (7×6) 350 (7×50) 120 (20×50) 1512

r 5	5.5 Short multiplication Abstract only but might need a repeat of year 4 first (up to 4 digit X 1 digit) https://www.youtube.com/watch? y=3YScfFlbWsQ	See Year 4 if required	See Year 4 if required	$ \begin{array}{c cccc} 2 & 7 & 4 & 1 \\ X & & 6 \\ \hline 1 & 6 & 4 & 4 & 6 \\ \hline 4 & 2 \end{array} $
Year	5.6 Long multiplication Abstract only but might need a repeat of year 4 first (up to 4 digit X 2 digits)		See year 4 if required.	132 × 56 7 92 (132 × 6) 6600 (132 × 50) 73 92
Year 6	6.5 Long multiplication Abstract method (up to 4 digits by a 2 digit number) https://www.youtube.com/watch? v=9gHHTOL5514		See year 4 if required.	132 × 56 792 (132 × 6) 6600 (132 × 50) 7392

Conceptual variation; different ways to ask children to solve 6 × 23



Division



Key language: share, group, groups of, lots of, regroup divide, divided by, remainder divisor, dividend.

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	Progression	Concrete	Pictorial	Abstract			
EYFS / Year 1	objects into groups. https://www.youtube.com/watch?v=a7RB-gesqAU 1.13 Division by making	6 ÷ 2	Represent the sharing pictorially. Pictures of objects	6 ÷ 2 = 3 3 3 12 ÷ 3 = 4			
EYF	groups. https://www.youtube.com/watch? v= l3f0526wC8	I have 12 strawberries and put them in groups of 3, how many groups?	Each pot needs three pencils in. How many pots do we need?				
ar 2	2.9 Division by making groups. https://www.youtube.com/watch? v=9aicYLZiL2A	18 in groups of 6.	18:6:3	There are 3 groups of 6 in 18. 18 ÷ 6 = 3			
Year	2.10 Division within arrays- linking to multiplication. (Sharing and grouping) https://www.youtube.com/watch? v=95Y4UCivcww	15 shared between 3. 15 in groups of 5.	15 ÷ 5 = 3 15 ÷ 3 = 5	$15 \div 5 = 3$ $15 \div 3 = 5$			

	2.11 Division as counting up https://www.youtube.com/watch? v=2c3FwEcCpyc	How many groups of 2 in 6? Use number line or Cuisenaire rods on a ruler. 6 ÷ 2 3 groups of 2	Children to represent division by counting up	6 ÷ 2 = 3
Year 3	number by a one digit number with and without remainders. https://www.youtube.com/watch? v=d0mB9lprpwQ	also be used. 13 ÷ 4 Use of lollipop sticks to form wholessquares are made because we are dividing by 4. There are 3 whole squares, with 1 remainder. Use of numicon. How many groups of 3 in 20? 20 ÷ 3	There are 3 whole squares, with 1 left over.	Children should be encouraged to use their times table facts; they could also represent repeated addition on a number line. '3 groups of 4, with 1 left over' $13 \div 4 = 3 \text{ r 1}$
	To divide a two digit	counters and dienes to group. $42 \div 3 = 14$	Children to represent the place value counters/dienes pictorially. 42 ÷ 3 = 14	$3\overline{4'2}$ $42 \div 3 = 14$

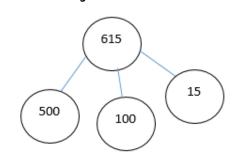
Year 4	4.5 Short division To divide a 3 digit number by a 1 digit number with regrouping in hundreds, tens and ones https://www.youtube.com/watch?	00000		Children progress to the calculation using the short division scaffold. $\frac{123}{5^{1}6^{1}5}$
	5.7 Short division Dividing a 4 digit number by a 1 digit number including remainders	How many groups of 5 hundreds can you make with 6 hundred counters? See Year 4 if required.	See Year 4 if required.	0 6 5 8. Remainder 2 4) 2 2 6 3 4
Year 5	5.8 Short division Division problems with decimal numbers (up to 2 d.p) https://www.youtube.com/wach?v=Jzolg7iqNog	0.1 0.1 0.1 0.0 0.0 0.0 0.0	0.8 ÷ 5 Ones 1 tenths to hundreths too Ones 1 tenths to hundreths too Ones 1 tenths to hundreths too	0.16 5)0.8³0

6.6 Short division	See Year 4 if required.	See Year 4 if required.	0 6 5 4) 2 °6°	
6.7 Long division/ chunking method (up to 4 digit by a 2 digit number) https://www.youtube.com/ watch?v=y6TmqkHIoOQ			203 14 2842 2800 - (200 × 14) 0042 0042 - (3 × 14)	Help Box 1×14 = 14 2×14 = 28 3×14 = 42 4×14 = 56 5×14 = 70 6×14 = 84 7×14 = 98 8×14 = 112 9×14 = 126 10×14 = 140

Conceptual variation; different ways to ask children to solve

Visual representations:

Using the part whole model below, how can you divide 615 by 5 without using short division?



Word problems:

I have £615 and share it equally between 5 bank accounts. How much will be in each account?

615 pupils need to be put into 5 groups. How many will be in each group?

Different forms of equation:

5 615

 $615 \div 5 =$

Concrete representations:

What is the calculation? What is the answer?

100s	10s	1s
000	00000	00000 00000