

Calculation progression map

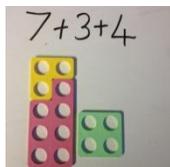
See White Rose Version 3 year group planning documents for a further detailed breakdown of calculation progression in each year group

Addition				
Key language: sum, total, parts and wholes, plus, add, altogether, more, 'is equal to', 'is the same as' and regrouping.				
Progression	Concrete	Pictorial	Abstract	
EYFS / Year 1	<p>1.1 Combining two parts to make a whole.</p>		<p>$4 + 3 = 7$ Four is a part, 3 is a part and the whole is seven.</p>	<p>$4 + 3 = 7$ Four is a part, 3 is a part and the whole is seven.</p>
	<p>1.2 Starting at the bigger number and counting on.</p>	<p>Counting on using number lines, cubes or Numicon.</p>	<p>A bar model which encourages the children to count on, rather than count all.</p>	<p>The abstract numberline: $4 + 2 = 6$</p>
	<p>1.3 Regrouping to make 10. Using ten frames and Numicon.</p>	<p>$6 + 5$</p>	<p>Children to draw the ten frame and counters/cubes.</p>	<p>Children to develop an understanding of equality e.g.</p> <p>$6 + \square = 11$ $6 + 5 = 5 + \square$ $6 + 5 = \square + 4$</p>

Year 2

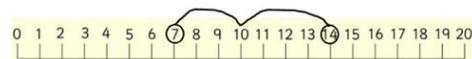
2.1 Adding three single digits.

Using Numicon or ten frames.



Using pictures of ten frames or number line.

$7 + 3 + 4$



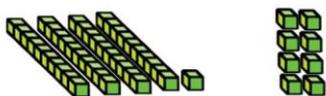
Using number bonds to make ten

$\underline{6} + 7 + \underline{4} = 6 + 4 + 7 = 17$

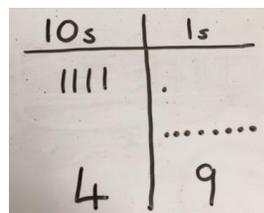
2.2 Use dienes to add two numbers.
(2 digit + 1 digit and 2 digit + 2 digit)

Continue to develop understanding of partitioning and place value.

$41 + 8$



Children to represent the dienes e.g. lines for tens and dot/crosses for ones.

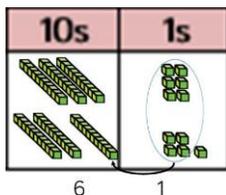


$41 + 8$

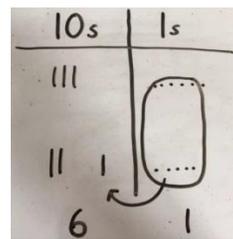
Add the ones: $1 + 8 = 9$
Add the tens: $40 + 9 = 49$

2.3 Use dienes to add two numbers with regrouping.
(2 digit + 1 digit and digit + 2 digit)

$36 + 25$
(regrouping in the ones)



$36 + 25$



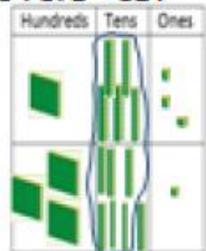
Expanded method: $36 + 25$

Add the ones: $6 + 5 = 11$
Add the tens: $30 + 20 = 50$
 $50 + 11 = 61$

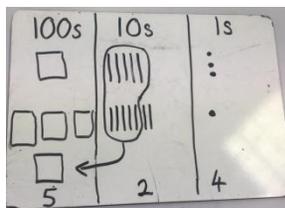
Year 3

3.1 Column method- regrouping
(up to 3 digits).
Using dienes.

$153 + 371 = 524$



$153 + 371 = 524$

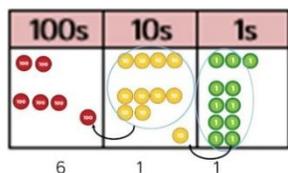


Introduce formal written method:

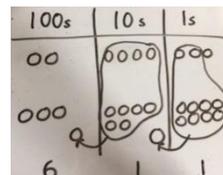
$$\begin{array}{r} 153 \\ + 371 \\ \hline 524 \\ 1 \end{array}$$

3.2 Column method- regrouping
(up to 3 digits).
Using place value counters.

$243 + 368 = 611$

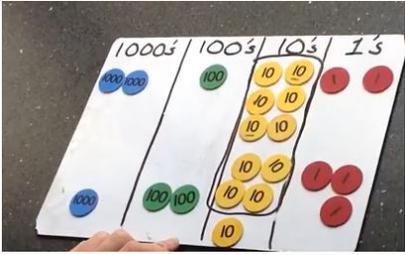
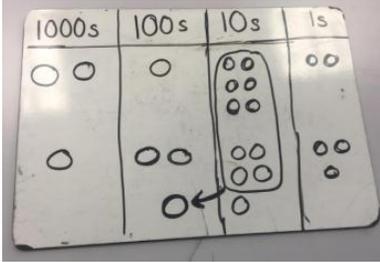
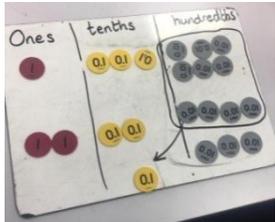
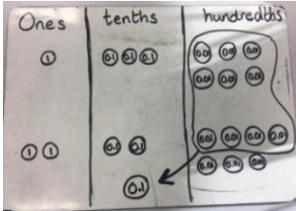


$243 + 368 = 611$



243

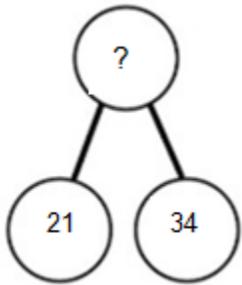
$$\begin{array}{r} 243 \\ + 368 \\ \hline 611 \\ 1 \quad 1 \end{array}$$

Year 4	<p>4.1 Column method- <u>regrouping</u> (up to 4 digits). Using place value counters.</p>	<p>2162 + 1253</p> 	<p>2162 + 1253</p> 	$\begin{array}{r} 2162 \\ + 1253 \\ \hline 3515 \\ 1 \end{array}$
Year 5	<p>5.1 Column method- <u>regrouping with more than 4 digits</u></p>	<p>See Year 4 if required.</p>	<p>See Year 4 if required.</p>	$\begin{array}{r} 1720\text{cm} \\ 750\text{cm} \\ + 1500\text{cm} \\ \hline 3970\text{cm} \\ 1 \end{array}$
Year 5	<p>5.2 Column method – decimals (up to 2 d.p.). Use place value counters.</p>	<p>1.36 + 2.37</p> 	<p>1.36 + 2.37</p> 	$\begin{array}{r} £1.36 \\ + £2.37 \\ \hline £3.73 \\ 1 \end{array}$
Year 6	<p>6.1 Column method- <u>regrouping with more than 4 digits</u></p>	<p>See Year 4 if required.</p>	<p>See Year 4 if required.</p>	$\begin{array}{r} 1720\text{cm} \\ 750\text{cm} \\ + 1500\text{cm} \\ \hline 3970\text{cm} \\ 1 \end{array}$
Year 6	<p>6.2 Column method – decimals (up to 2 d.p.). Use place value counters.</p>	<p>See Year 5 if required.</p>	<p>See Year 5 if required.</p>	$\begin{array}{r} £1.36 \\ + £2.37 \\ \hline £3.73 \\ 1 \end{array}$

Conceptual variation - different ways to ask children to solve 21+34

Visual representations:

Part-part-whole diagrams and bar models.



?	
21	34

Word problems:

In year 3, there are 21 children and in year 4, there are 34 children.
How many children in total?

Calculate the sum of twenty-one and thirty-four.

Different forms of equations:

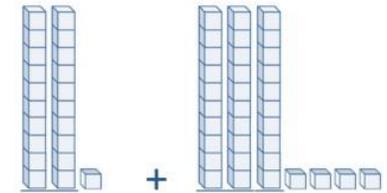
$$\begin{array}{r} 21 \\ +34 \\ \hline \end{array}$$

$$21 + 34 =$$

$$\square = 21 + 34$$

21 + 34 = 55. Prove it

Concrete representations:



Missing digit problems:

10s	1s
10 10	1
10 10 10	?
?	5

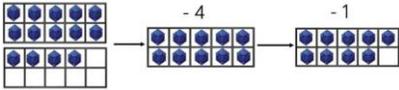
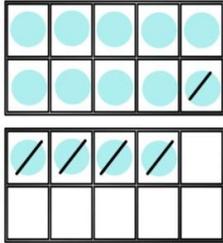
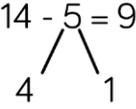
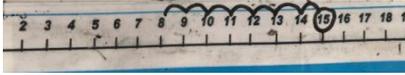
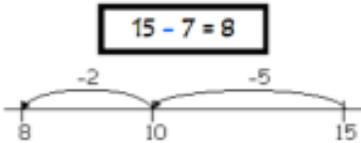
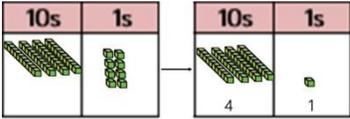
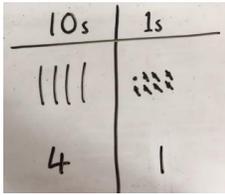
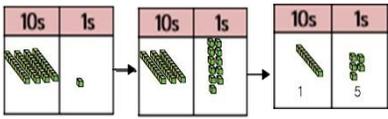
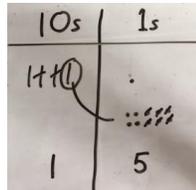
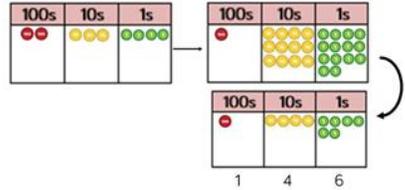
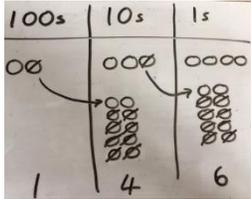
Subtraction

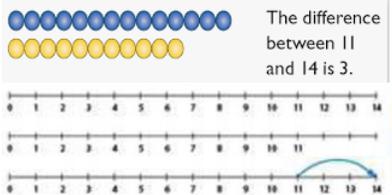
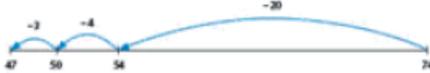
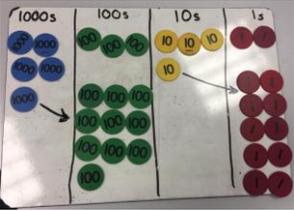
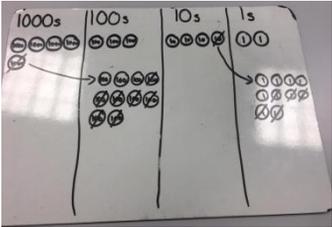
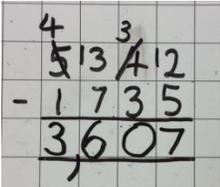
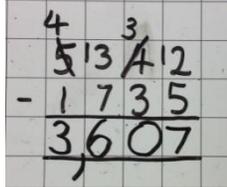
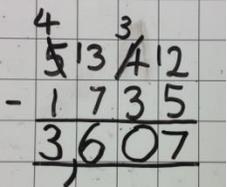
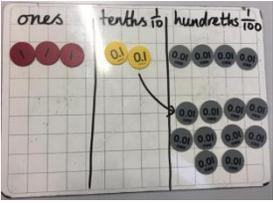
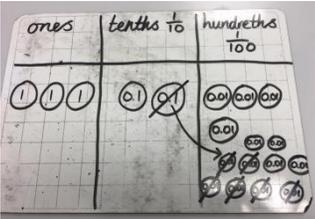
Key language: take away, less than, difference, subtract, minus, fewer, decrease, reduce.



EYFS / Year 1

Progression	Concrete	Pictorial	Abstract
<p>1.4 Taking away ones from a whole.</p>	<p>Physically taking away objects from a whole.</p> <p>$4 - 3 = 1$</p>	<p>Children to draw the concrete resources they are using and cross out the correct amount. The bar model can also be used.</p>	<p>$4 - 3 =$ <input style="width: 30px; height: 20px;" type="text"/></p> <p><input style="width: 30px; height: 20px;" type="text"/> $= 4 - 3$</p>
<p>1.5 Counting back using a number line.</p>	<p>Counting back (using number lines or number tracks) children start with 6 and count back 2.</p> <p>$6 - 2 = 4$</p>	<p>$6 - 2 = 4$</p>	<p>$6 - 2 = 4$</p>
<p>1.6 Find the difference by counting on.</p>	<p>Finding the difference (using cubes, Numicon or Cuisenaire rods).</p> <p>Find the difference between 8 and 5.</p>	<p>Children to draw the concrete resources they have used or used a bar model to illustrate what they need to calculate.</p>	<p>Find the difference between 8 and 5.</p> <p>$5 + 3 = 8$</p>

	<p>1.7 Make 10 using the ten frame</p>	<p>Making 10 using a ten frame. $14 - 5$</p> 	<p>Children to present the ten frame pictorially and discuss what they did to make ten.</p> 	<p>Children to show how they can make ten by partitioning the smaller number.</p> $14 - 5 = 9$  $14 - 4 = 10$ $10 - 1 = 9$
Year 2	<p>2.4 Counting back using a number line.</p>	<p>$15 - 7$</p> 		<p>$15 - 7 = 8$</p>
	<p>2.5 Use dienes to subtract numbers up to 2 digits (without regrouping).</p>	<p>Column method using dienes. $48 - 7$</p> 	<p>Children to represent dienes pictorially.</p> 	<p>$48 - 7 = 41$</p>
	<p>2.6 Use dienes to subtract numbers up to 2 digits (with regrouping).</p>	<p>Column method using dienes. $41 - 26$</p> 	<p>$41 - 26$</p> 	<p>$41 - 26 = 15$</p>
Year 3	<p>3.3 Column method with regrouping. Using place value counters and dienes up to 3 digits.</p>	<p>Column method using place value counters. $234 - 88$</p> 	<p>$234 - 88$</p> 	<p>Formal column written method.</p> $\begin{array}{r} 234 \\ - 88 \\ \hline 146 \end{array}$

	3.4 Finding the difference	<p>Begin to find the difference by counting on or back.</p>  <p>The difference between 11 and 14 is 3.</p>	<p>$74 - 47 = 27$</p> 	<p>$74 - 47 = 27$</p>
Year 4	<p>4.2 Column method with regrouping (including regrouping thousands, hundreds, tens and ones). Up to 4 digits using place value counters.</p>	<p>5342 – 1735</p> 	<p>5342 – 1735</p> 	<p>5342 – 1735</p> 
Year 5	<p>5.3 Abstract column method with regrouping (including numbers with more than 4 digits).</p>	<p>See Year 4 if required.</p>	<p>See Year 4 if required.</p>	<p>5342 – 1735</p> 
Year 6	<p>6.3 Abstract column method with regrouping (including numbers with more than 4 digits).</p>	<p>See Year 4 if required.</p>	<p>See Year 4 if required.</p>	<p>5342 – 1735</p> 
Year 5	<p>5.4 Column method for decimals up to 2 decimal places with place value counters.</p>	<p>3.24 – 1.16</p> 	<p>3.24 – 1.16</p> 	<p>$\pounds 3.18^4$</p> <p>$-\pounds 1.16$</p> <hr/> <p>$\pounds 2.08$</p>

[6.4 Column method for decimals up to 2 decimal places with place value counters](#)

See Year 5 if required.

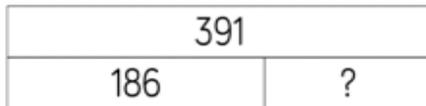
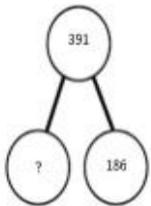
See Year 5 if required.

See Year 5 if required.

Conceptual variation - different ways to ask children to solve $391 - 186$

Visual representations:

Part-part-whole diagrams and bar models.



Word problems:

Raj spent £391, Timmy spent £186.
How much more did Raj spend?

Calculate the difference between 391 and 186.

Different forms of equations:

391

-186

What is 186 less than 391?

Missing digit calculations

$$\begin{array}{r}
 39\boxed{} \\
 - \boxed{}\boxed{}6 \\
 \hline
 \boxed{}05
 \end{array}$$

391 - 186

Concrete representations:

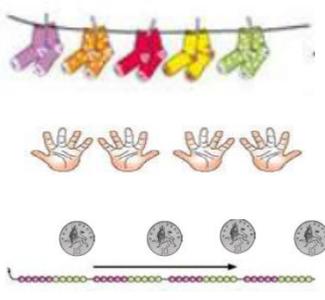
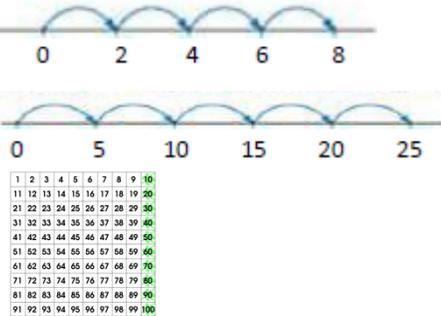
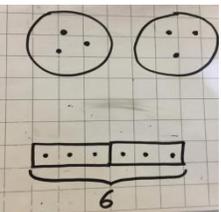
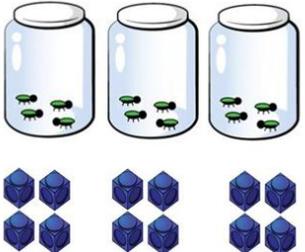
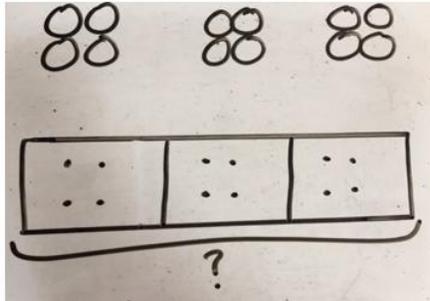


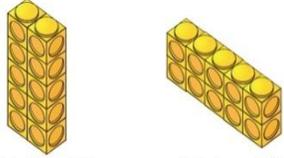
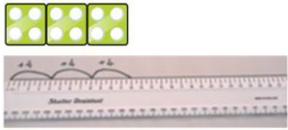
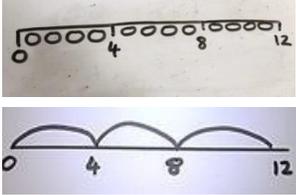
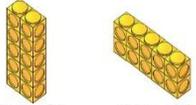
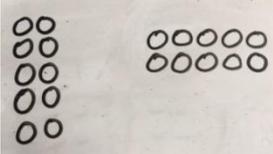
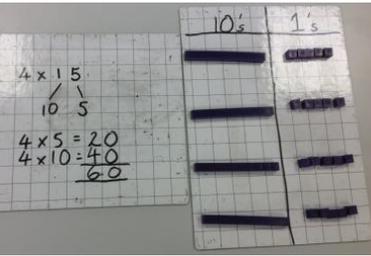
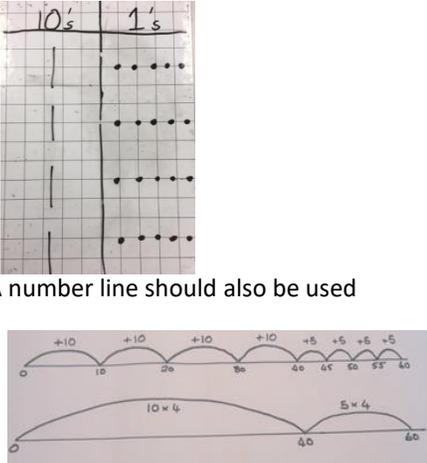
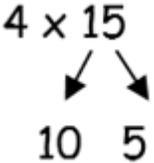
The difference between 11 and 14 is 3.

Multiplication

Key language: double, times, multiplied by, the product of, groups of, lots of, equal groups, factors, regroup.

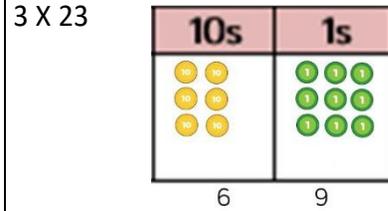
Year 1/ EYFS

Progression	Concrete	Pictorial	Abstract
1.8 Counting in multiples (skip count in 2's, 5's and 10's)			"5, 10, 15, 20, 25..."
1.9 Doubling			$3 + 3 = 6$
1.10 Repeated addition.	<p>Repeated addition 3×4 $4 + 4 + 4$ There are 3 equal groups, with 4 in each group.</p> 	<p>Children to represent the practical resources in a picture and use a bar model.</p> 	$3 \times 4 = 12$ $4 + 4 + 4 = 12$

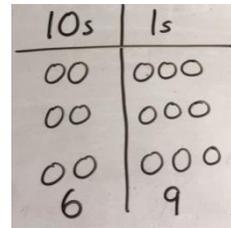
	<p>1.11 Arrays</p>	<p>Putting objects into arrays. $2 \times 5 = 5 \times 2$</p>  <p>2 lots of 5 5 lots of 2</p>	<p>Children describe arrays in different ways. 2 groups of 5 5 groups of 2</p> 	<p>Children to be able to use an array to write a range of calculations e.g.</p> <p>$5 \times 2 = 10$ $2 \times 5 = 10$ $10 = 2 \times 5$ $10 = 5 \times 2$</p>
<p style="writing-mode: vertical-rl; transform: rotate(180deg);">Year 2</p>	<p>2.7 Number line to show repeated addition</p>	<p>Number lines to show repeated groups. E.g. 3×4</p>  <p>Cuisenaire rods and Numicon can be used too.</p>	<p>Represent this pictorially alongside a number line</p> 	<p>$4 + 4 + 4 = 12$ $3 \times 4 = 12$</p>
	<p>2.8 Arrays - showing commutative multiplication</p>	<p>Use arrays to illustrate commutativity counters and pegs can be used. $2 \times 5 = 5 \times 2$</p>  <p>2 lots of 5 5 lots of 2</p>	<p>Children to represent the arrays pictorially.</p> <p>2×5 5×2</p> 	<p>Children to be able to use an array to write a range of calculations e.g.</p> <p>$10 = 2 \times 5$ $5 \times 2 = 10$ $2 + 2 + 2 + 2 + 2 = 10$ $10 = 5 + 5$</p>
<p style="writing-mode: vertical-rl; transform: rotate(180deg);">Year 3</p>	<p>3.5 Multiplication by partitioning $2d \times 1d$ using dienes</p>	<p>Partition to multiply using dienes of Numicon.</p> 	<p>4×15</p>  <p>A number line should also be used</p>	<p>Children to be encouraged to show the steps they have taken.</p> <p>4×15</p>  <p>$4 \times 5 = 20$ $4 \times 10 = 40$ <u>60</u></p>

3.6 Short multiplication (2 digit X 1 digit)

Short multiplication method.
Use counters or dienes.



3 X 23

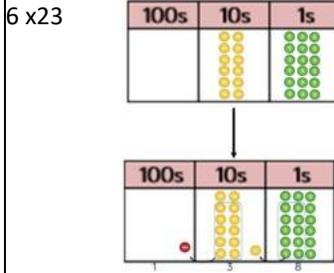


Children to be encouraged to show the steps they have taken.

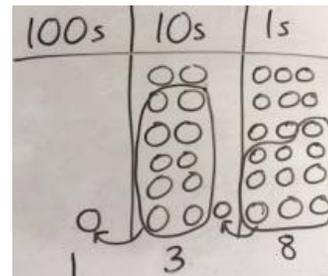
$$\begin{array}{r} 3 \times 3 = 9 \\ 3 \times 20 = 60 \\ \hline 69 \end{array} \qquad \begin{array}{r} 23 \\ \times 3 \\ \hline 69 \end{array}$$

3.7 Short multiplication with regrouping (2 digit X 1 digit)

Formal column method with place value counters.



6 X 23

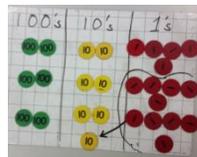


Formal written method

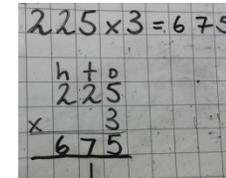
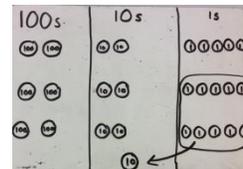
$$\begin{array}{r} 6 \times 23 = \\ 23 \\ \times 6 \\ \hline 138 \\ 1 \quad 1 \end{array}$$

4.3 Short multiplication- place value counters. (2 and 3 digit X 1 digit)

225 X 3 = 675



225 X 3 = 675



4.4 Grid method to expanded method. (for 2- digit X 2-digit)

Use abstract methods.

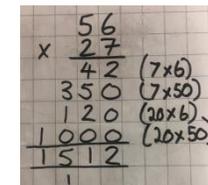
Use abstract methods.

First introduce children to the grid method.

56 x 27 = 1512

x	20	7	
50	1000	350	1350
6	120	42	162
			1512

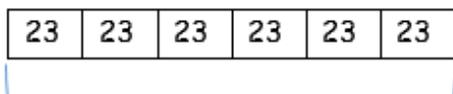
Then progress to the expanded method.



Year 5	5.5 Short multiplication <u>Abstract only but might need a repeat of year 4 first (up to 4 digit X 1 digit)</u>	See Year 4 if required	See Year 4 if required	
	5.6 Long multiplication <u>Abstract only but might need a repeat of year 4 first (up to 4 digit X 2 digits)</u>	See year 4 if required.	See year 4 if required.	$\begin{array}{r} 132 \\ \times 56 \\ \hline 792 \quad (132 \times 6) \\ 6600 \quad (132 \times 50) \\ \hline 7392 \end{array}$
Year 6	6.5 Long multiplication <u>Abstract method (up to 4 digits by a 2 digit number)</u>	See year 4 if required.	See year 4 if required.	$\begin{array}{r} 132 \\ \times 56 \\ \hline 792 \quad (132 \times 6) \\ 6600 \quad (132 \times 50) \\ \hline 7392 \end{array}$

Conceptual variation - different ways to ask children to solve 6×23

Visual representations:



?

This image shows 4×6



Change the image to show 4×7

Word problems:

Mai had to swim 23 lengths, 6 times a week.
How many lengths did she swim in one week?

Using place value counters, prove
prove that $6 \times 23 = 138$

Different forms of equation:

Find the product of 6 and 23

$$\square 6 \times 23$$

$$\begin{array}{r} 6 \quad 23 \\ \times 23 \quad \times 6 \\ \hline \quad \quad \hline \end{array}$$

Concrete representations:

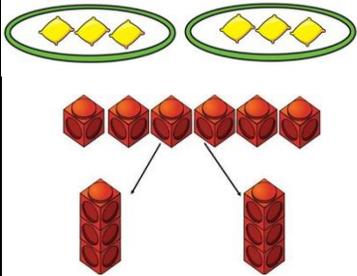
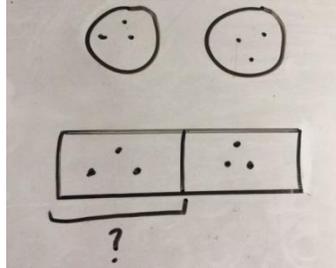
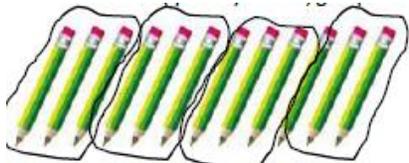
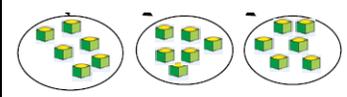
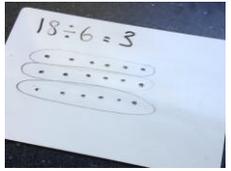
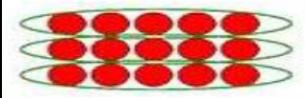
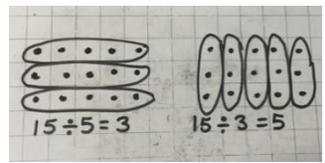
What is the calculation? What is the product?

100s	10s	1s
	●● ●● ●● ●●	●●●● ●●●● ●●●● ●●●●

Division

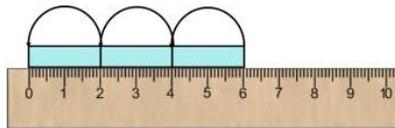
Key language: share, group, equal group, groups of, lots of, regroup, divide, divided by, remainder, divisor, dividend, quotient



	Progression	Concrete	Pictorial	Abstract		
EYFS / Year 1	1.12 Division by sharing objects into groups.	Sharing using a range of objects. $6 \div 2$ 	Represent the sharing pictorially. 	$6 \div 2 = 3$ <table border="1" style="width: 100%; text-align: center;"> <tr> <td style="width: 50%;">3</td> <td style="width: 50%;">3</td> </tr> </table>	3	3
	3	3				
1.13 Division by making groups.	I have 12 strawberries and put them in groups of 3, how many groups? 	Pictures of objects Each pot needs three pencils in. How many pots do we need? 	$12 \div 3 = 4$			
Year 2	2.9 Division by making groups.	18 in groups of 6. 		There are 3 groups of 6 in 18. $18 \div 6 = 3$		
	2.10 Division within arrays- linking to multiplication. (Sharing and grouping)	15 shared between 3. 15 in groups of 5. 		$15 \div 5 = 3$ $15 \div 3 = 5$		

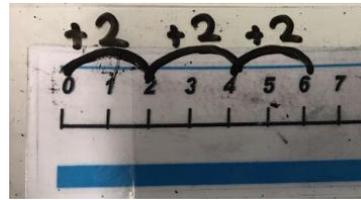
2.11 Division as counting up

How many groups of 2 in 6?
Use number line or Cuisenaire rods on a ruler.
 $6 \div 2$



3 groups of 2

Children to represent division by counting up



$6 \div 2 = 3$

3.8 To divide a two digit number by a one digit number with and without remainders.

Cuisenaire rods, above a ruler can also be used.
 $13 \div 4$

Use of lollipop sticks to form wholes-squares are made because we are dividing by 4.



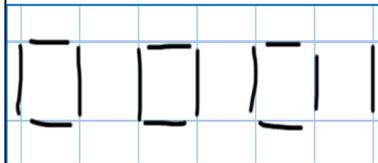
There are 3 whole squares, with 1 remainder.

Use of numicon. How many groups of 3 in 20?

$20 \div 3$



Children to represent the lollipop sticks pictorially.



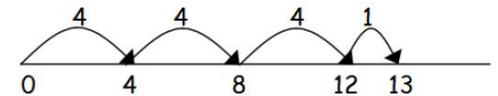
There are 3 whole squares, with 1 left over.

$13 \div 4 = 3 \text{ remainder } 1$

Children should be encouraged to use their times table facts; they could also represent repeated addition on a number line.

'3 groups of 4, with 1 left over'

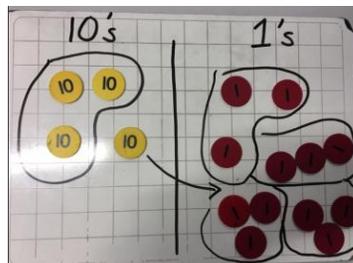
$13 \div 4 = 3 \text{ r } 1$



3.9 Short Division
To divide a two digit number by a one digit number with regrouping of tens and ones (no remainders)

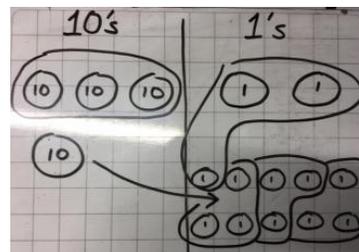
Short division using place value counters and dienes to group.

$42 \div 3 = 14$



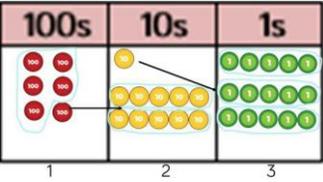
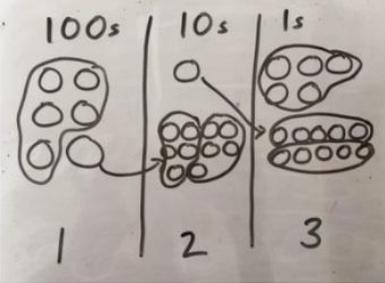
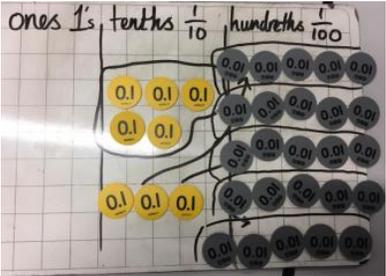
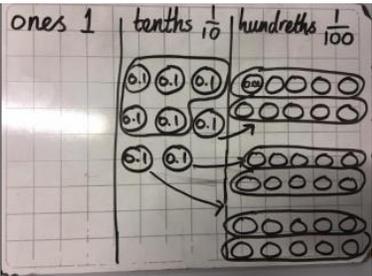
Children to represent the place value counters/dienes pictorially.

$42 \div 3 = 14$



$$\begin{array}{r} 14 \\ 3 \overline{)42} \\ \underline{30} \\ 12 \\ \underline{12} \\ 0 \end{array}$$

 $42 \div 3 = 14$

<p style="writing-mode: vertical-rl; transform: rotate(180deg);">Year 4</p>	<p>4.5 Short division To divide a 3 digit number by a 1 digit number with regrouping in hundreds, tens and ones</p>	<p>Short division using place value counters to <u>group</u>. $615 \div 5$</p>  <p>How many groups of 5 hundreds can you make with 6 hundred counters?</p>	<p>Represent the place value counters pictorially.</p> 	<p>Children progress to the calculation using the short division scaffold.</p> $\begin{array}{r} 123 \\ 5 \overline{) 615} \end{array}$
<p style="writing-mode: vertical-rl; transform: rotate(180deg);">Year 5</p>	<p>5.7 Short division Dividing a 4 digit number by a 1 digit number including remainders</p>	<p>See Year 4 if required.</p>	<p>See Year 4 if required.</p>	$\begin{array}{r} 0658. \\ 4 \overline{) 2^26^23^34} \end{array}$ <p style="text-align: right;">Remainder 2</p>
<p style="writing-mode: vertical-rl; transform: rotate(180deg);">Year 5</p>	<p>5.8 Short division Division problems with decimal numbers (up to 2 d.p)</p>	<p>$0.8 \div 5$</p> 	<p>$0.8 \div 5$</p> 	$\begin{array}{r} 0.16 \\ 5 \overline{) 0.8^30} \end{array}$
<p style="writing-mode: vertical-rl; transform: rotate(180deg);">Year 6</p>	<p>6.6 Short division</p>	<p>See Year 4 if required.</p>	<p>See Year 4 if required.</p>	$\begin{array}{r} 0658. \\ 4 \overline{) 2^26^23^34} \end{array}$

6.7 Long division/ chunking method (up to 4 digit by a 2 digit number)

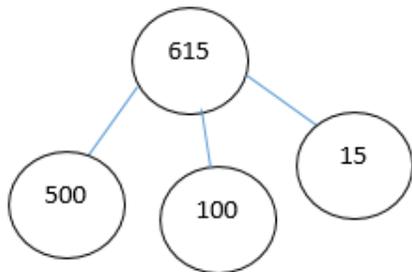
$$\begin{array}{r}
 203 \\
 14 \overline{) 2842} \\
 \underline{2800} - (200 \times 14) \\
 0042 \\
 \underline{0042} - (3 \times 14) \\
 0000
 \end{array}$$

Help Box	
1x14 =	14
2x14 =	28
3x14 =	42
4x14 =	56
5x14 =	70
6x14 =	84
7x14 =	98
8x14 =	112
9x14 =	126
10x14 =	140

Conceptual variation - different ways to ask children to solve $615 \div 5$

Visual representations:

Using the part whole model below, how can you divide 615 by 5 without using short division?



Word problems:

I have £615 and share it equally between 5 bank accounts. How much will be in each account?

615 pupils need to be put into 5 groups. How many will be in each group?

Different forms of equation:

$$5 \overline{) 615}$$

$$615 \div 5 =$$

$$\square = 615 \div 5$$

Concrete representations:

What is the calculation?
What is the answer?

